

LECTURE 1.3



# VARs: Applications and Identification

ECON42240 Advanced Macroeconomics

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# Where We Are

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## 1. Time Series Methods

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1.1 Time Series and Macro

1.2 Vector Autoregressions

**1.3 VARs: Applications**

1.4 The Kalman Filter

1.5 Solving RE Models

## 2. Structural Models

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2.1 The RBC Model

2.2 The Phillips Curve

2.3 The New Keynesian Model

2.4 Estimating DSGE Models

2.5 The Smets-Wouters Model

## 3. Finance and Policy

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3.1 Credit and Banking Crises

3.2 Fiscal Policy, and What Next

# Last Week's Lecture

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## 1 Specifying a VAR.

Which variables, how many lags, on what data.

## 2 Estimating a VAR.

Equation by equation, by least squares.

## 3 Reading the Output.

Impulse responses, error bands and variance shares.

## 4 Residuals and Structural Shocks.

Why every mix of shocks fits the data.

# Lecture Plan

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## 1 The Identification Problem.

Why residuals are not shocks.

## 2 Recursive Identification.

What a Cholesky ordering assumes.

## 3 Monetary Policy Shocks.

Why the ordering can decide the answer.

## 4 Long-Run Restrictions.

Identifying technology shocks instead.

## SECTION 1

# The Identification Problem

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1. The Identification Problem
2. Recursive Identification
3. Monetary Policy Shocks
4. Long-Run Restrictions

# A Residual Is Not a Structural Shock

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Each residual ( $e_{it}$ ) is a forecast error, not an economic event:

- **What Least Squares Returns:** The part of each variable the VAR's lags miss.
- **What Theory Defines:** A named disturbance, from policy, technology or preferences.
- **Why the Two Differ:** One economic surprise arrives in several equations at once.

## A Structural Shock Has an Economic Name

A structural shock is an exogenous disturbance to one behavioural relation. Each residual mixes several such shocks.

## Two Ways to Write the Same System

The structural form keeps the within-period effects ( $A_0$ ) on the left:

$$A_0 Z_t = \sum_{i=1}^p A_i Z_{t-i} + \varepsilon_t \quad (1)$$

where:

- $Z_t$ : vector of the  $n$  variables
- $p$ : number of lags
- $A_i$ : coefficients on lag  $i$

### Only the Reduced Form Can Be Estimated

Current variables on the right correlate with the equation's shock ( $\varepsilon_t$ ).

# What the Residuals Mix Together

Pre-multiplying by  $A_0^{-1}$  leaves only lags on the right, so least squares works:

$$Z_t = \sum_{i=1}^p A_0^{-1} A_i Z_{t-i} + \underbrace{A_0^{-1} \varepsilon_t}_{e_t} \quad (2)$$

## Every Estimate Carries the Same Unknown Inverse

Least squares returns  $A_0^{-1} A_i$  and  $A_0^{-1} \varepsilon_t$ , never  $A_i$  or  $\varepsilon_t$ . Each residual is a weighted sum of structural shocks.

# One Lag Keeps the Algebra Short

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With one lag, write the impact matrix ( $C$ ) for  $A_0^{-1}$ :

$$Z_t = BZ_{t-1} + C\varepsilon_t \quad (3)$$

where:

- $B$ : reduced-form lag matrix

## Each Entry Is One Impact Effect

$c_{ij}$  is shock  $j$ 's effect on variable  $i$  in the period it arrives. Stacking more lags in companion form changes nothing here.

# The Covariance Matrix Is the Only Evidence

Assume the structural shocks are uncorrelated, and scale each to unit variance:

$$\Sigma \equiv E(e_t e_t') = CC' \quad (4)$$

## Estimation Stops at the Covariance Matrix

Least squares delivers the residual covariance ( $\Sigma$ ) and nothing more about  $C$ . Identification is the set of assumptions supplying the rest.

## Identification Needs $n(n-1)/2$ Restrictions

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$C$  holds more unknowns than the symmetric  $\Sigma$  holds distinct numbers:

$$\underbrace{n^2}_{\text{unknowns in } C} - \underbrace{n(n+1)/2}_{\text{numbers in } \Sigma} = n(n-1)/2 \quad (5)$$

**1**

restriction with two variables

**3**

restrictions with three variables

# Restrictions Come from Outside the Data

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Each scheme closes the gap with a claim the sample cannot test:

- **Timing:** One variable cannot be changed within the period by another.
- **Sign:** A shock raises one variable and lowers another on impact.
- **The Long Run:** One shock has no permanent effect on one variable.

## A Just-Identified Scheme Cannot Be Tested

Exactly  $n(n - 1)/2$  restrictions leave no slack. Every just-identified scheme fits the data equally well.

## Naming a Shock Before Identifying It

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The real oil price rose through the 2000s, and sharply again in 2022.

### **Question**

What restriction would let you call the 2022 rise supply rather than demand? Name it.

Take answers from the room.

## SECTION 2

# Recursive Identification

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1. The Identification Problem
2. Recursive Identification
3. Monetary Policy Shocks
4. Long-Run Restrictions

## An Ordering Supplies the Missing Restrictions

With two variables, a shock ordered second cannot enter the first residual:

$$\begin{pmatrix} e_{1t} \\ e_{2t} \end{pmatrix} = \begin{pmatrix} c_{11} & 0 \\ c_{21} & c_{22} \end{pmatrix} \begin{pmatrix} \varepsilon_{1t} \\ \varepsilon_{2t} \end{pmatrix} \quad (6)$$

### Recursive Means Ordered by Within-Period Effects

A recursive system orders the variables so that  $A_0$  is lower triangular. Its inverse,  $C$ , is then lower triangular too.

# Cholesky Delivers the Triangular Matrix

An ordering fixes which entries of  $C$  are zero. One matrix fact fixes the rest:

$$\Sigma = PP' \quad (7)$$

where:

- $P$ : lower-triangular Cholesky factor

## One Factor, with Exactly the Missing Zeros

Only one such  $P$  has a positive diagonal, which pins down  $C = P$ . Its  $n(n - 1)/2$  zeros close the gap exactly.

## Kilian Asks What an Oil Price Shock Is

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Oil price run-ups precede many recessions, though oil is a small input. Kilian asks a prior question (Kilian, 2009):

- **The Old Question:** What are the effects of an oil price shock?
- **Kilian's Question:** What kind of oil price shock is this one?
- **Three Candidates:** Oil supply, global demand, and speculation in the oil market.

## Kilian's Three-Variable Monthly VAR

Three monthly series, twenty-four lags, and an ordering argued from oil markets (Kilian, 2009):

$$z_t = (\Delta\text{prod}_t, \text{rea}_t, \text{rpo}_t)', \quad A_0 z_t = \sum_{i=1}^{24} A_i z_{t-i} + \varepsilon_t \quad (8)$$

where:

- $z_t$ : Kilian's three variables
- $\Delta\text{prod}_t$ : growth of world oil output
- $\text{rea}_t$ : global real activity index
- $\text{rpo}_t$ : real price of oil

## Kilian's Three Identifying Restrictions

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Each zero is argued from how oil markets work; the data cannot test it:

$$A_0 = \begin{pmatrix} a & 0 & 0 \\ b & c & 0 \\ d & e & f \end{pmatrix} \quad (9)$$

- 1. Oil Supply First:** Within the month, neither demand nor price changes oil production.
- 2. Activity Second:** Oil production enters world demand at once, the price does not.
- 3. Price Last:** Oil production and world demand both enter the price at once.

## Counting Kilian's Identifying Restrictions

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$C$  holds nine unknowns and  $\Sigma$  six numbers, so three restrictions are missing:

### Three Zeros Close a Gap of Three

Kilian's three zeros above the diagonal fill the gap exactly. No restriction is left over to test.

A different ordering therefore fits the same data equally well.

## What the Residuals Mean Under This Ordering

A triangular  $A_0$  makes  $C$  triangular. Each residual mixes its own shock and those ordered above it:

$$\begin{pmatrix} e_t^{\text{prod}} \\ e_t^{\text{rea}} \\ e_t^{\text{rpo}} \end{pmatrix} = \begin{pmatrix} c_{11} & 0 & 0 \\ c_{21} & c_{22} & 0 \\ c_{31} & c_{32} & c_{33} \end{pmatrix} \begin{pmatrix} \varepsilon_t^{\text{prod}} \\ \varepsilon_t^{\text{rea}} \\ \varepsilon_t^{\text{rpo}} \end{pmatrix} \quad (10)$$

### Only the First Residual Is One Shock

The production residual is proportional to the oil supply shock. The other two residuals are the mixtures the ordering specifies.

# Decomposing the Oil Price into Its Shocks

A historical decomposition splits each month's oil price among the identified shocks:

$$Z_t = C\varepsilon_t + BC\varepsilon_{t-1} + B^2C\varepsilon_{t-2} + \dots \quad (11)$$

- 1. One Shock at a Time:** Set the other two shock series to zero.
- 2. Add the Three Paths:** The three paths and the initial conditions sum to the series.
- 3. Read the Attribution:** Each month's price splits into three named contributions.

## A Decomposition Needs the Realised Shocks

An impulse response traces one hypothetical shock. A decomposition feeds in every realised shock. Lecture 1.2 derived this moving-average form.

# The Real Oil Price and Its Three Shocks



**Figure 1:** Cumulative effect of each identified shock on the real oil price, 1976–2026.

## Supply Shocks Stay Small Throughout

Global demand accounts for most of the 2002–2008 climb. Speculative demand accounts for most of the 2022 spike.

# What Kilian's Three Shocks Explain

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On his own sample, Kilian finds the three shocks matter very unequally (Kilian, 2009):

- **Supply Shocks:** Negligible for oil prices over time.
- **Speculative Shocks:** Can be significant for oil prices, limited for global activity.
- **The 2000s Run-Up:** Almost solely strong global demand.

## An Oil Price Rise Has No Single Effect

An economy's path after an oil price rise depends on its cause. The cause helps explain a 2000s oil climb with no recession.

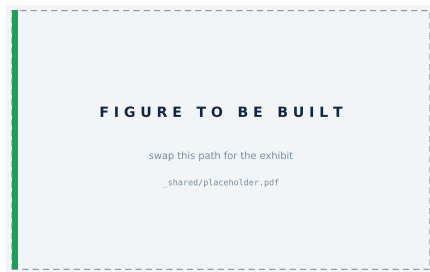
## Blanchard and Perotti on Fiscal Policy

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Blanchard and Perotti close the same gap partly with outside evidence (O. Blanchard & Perotti, 2002):

- **Spending Is Slow:** Legislating a reply to a GDP surprise takes months.
- **Taxes Are Mechanical:** Estimated elasticities fix the same-quarter effect of GDP.
- **Output Is Last:** Both taxes and spending enter GDP within the same quarter.

# GDP After a Tax Rise and a Spending Rise



**Figure 2:** Blanchard and Perotti's GDP responses to a tax rise and a spending rise.

**A Tax Rise Lowers GDP and a Spending Rise Raises It**

The two paths differ in shape and in timing, not only in sign.

# What Would a Monetary Policy Shock Be?

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A central bank sets its rate after looking at the economy.

## **Question**

Which part of a rate decision could count as a policy shock? Say why.

Take answers from the room.

## SECTION 3

# Monetary Policy Shocks

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1. The Identification Problem
2. Recursive Identification
3. Monetary Policy Shocks
4. Long-Run Restrictions

## A Monetary Policy VAR Has Two Uses

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Stock and Watson use a monetary VAR to answer two different questions (Stock & Watson, 2001):

- **The Scientific Question:** Only an exogenous policy change reveals policy's effects.
- **The Policy Question:** What follows a quarter-point rise beyond the bank's own rule?

### Only the Part Outside the Rule Identifies an Effect

Much of a rate change is the bank following its own rule. Only the remainder identifies an effect.

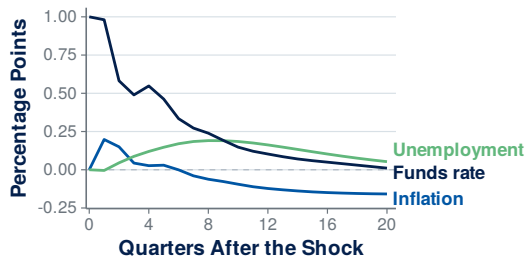
## Stock and Watson's Ordering

Inflation, unemployment and the funds rate, one restriction per row (Stock & Watson, 2001):

$$\begin{pmatrix} a_{11} & 0 & 0 \\ a_{21} & a_{22} & 0 \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \begin{pmatrix} \pi_t \\ u_t \\ i_t \end{pmatrix} = A_1 Z_{t-1} + \dots + A_p Z_{t-p} + \varepsilon_t \quad (12)$$

- 1. Inflation First ( $\pi_t$ ):** Sticky prices keep inflation free of within-quarter effects.
- 2. Unemployment Second ( $u_t$ ):** Current inflation enters unemployment, rates do not.
- 3. The Funds Rate Last ( $i_t$ ):** The Fed sees current inflation and unemployment.

# Impulse Responses from the First Ordering



**Figure 3:** Responses to a one-point funds rate rise, first ordering, 1960–2007.

## Inflation Rises for Five Quarters Before It Falls

Unemployment peaks about two years after the rise. Inflation stays above zero for five quarters, then falls below.

## A Rate Rise Appears to Raise Inflation

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In the first ordering, unemployment rises and inflation eventually falls, as theory predicts:

### **The Price Puzzle Is Inflation Rising First**

The price puzzle is inflation rising for several quarters after a rate rise. Several VAR studies find the puzzle.

Whether the short-run rise is an effect or a failure is disputed.

## Why the Price Puzzle Might Appear

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The Fed watches more than a three-variable VAR contains, commodity prices especially:

- **What the Fed Sees:** Signals of future inflation that the small VAR omits.
- **What the VAR Records:** Rate rises arriving shortly before inflation rises.
- **The Confusion:** One omitted signal explains both, so correlation reads as causation.

**Adding Commodity Prices Often Removes the Puzzle**

Better specification, or data mining for the wanted result?

## A Second Ordering, Equally Arguable

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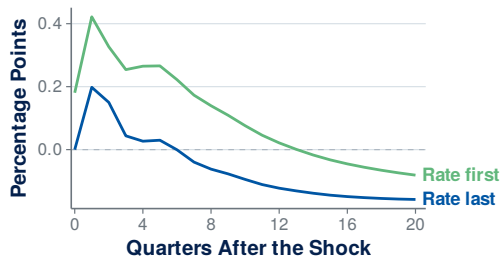
Three variables allow six orderings. Put the funds rate first and inflation last:

- **Why Rates First:** The Fed acts on lagged data, not on this quarter's.
- **Why Inflation Last:** Prices can change at once when economic conditions change.

### A Sensible-Looking Result Is Not Evidence

Which ordering a researcher keeps may depend on which results look sensible.

# The Same VAR Under Two Orderings



**Figure 4:** Inflation's response to a one-point funds rate rise, two orderings, 1960–2007.

## Putting the Rate First Stretches the Puzzle

Data, lags and sample are identical. With the rate first, inflation stays above zero through quarter 13, not quarter 5.

## Is This Data Mining?

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Two orderings are defensible and one gives sensible answers. Adding commodity prices often removes the puzzle too.

### **Question**

You have two orderings and one looks sensible. What would justify keeping the sensible one?

Take answers from the room.

## Only Outside Evidence Can Rank Two Orderings

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Both orderings fit the data identically, so the ranking needs outside evidence:

### **Report Both Orderings and Say Why**

Report both sets of responses. State which ordering you prefer, and on what evidence.

Institutional timing, or an elasticity measured elsewhere, counts as evidence.

# Rudebusch's Case Against Monetary VARs

Rudebusch argues that VAR monetary policy shocks are not policy surprises (Rudebusch, 1998):

- **The Rule Changed:** VARs impose one policy rule across decades of different regimes.
- **The Data Are Wrong:** VARs use revised figures the Fed never had.
- **The Information Is Thin:** The Fed watches far more than a VAR holds.
- **The Shocks Differ:** VAR shocks look nothing like fed funds futures surprises.

## Similar Responses from Very Different Shocks

Models with quite different shock series report similar impulse responses. Rudebusch suspects data mining.

# Sims's Reply to Rudebusch

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Sims accepts the questions and rejects the conclusion (Sims, 1998):

- **Different Shocks:** Two models can size shocks differently and still agree on effects.
- **A Surprise Is Not Exogeneity:** A pre-announced rate rise is still exogenous policy.
- **The Faults Are General:** Linearity and variable choice afflict every macro model.

## A Shock Measure Can Be Wrong and Still Useful

Sims argues an estimated effect can survive a mis-measured shock. The responses are what the exercise is for.

## Romer and Romer Build Shocks from the Record

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A narrative approach identifies policy shocks outside the VAR altogether (Romer & Romer, 2004):

- 1. The Intended Rate:** Internal Fed documents give the policy rate the Fed intended.
- 2. The Fed's Forecasts:** Internal forecasts of inflation and real activity, by meeting.
- 3. The Residual:** Regress the intended rate change on those forecasts, keep the rest.

# What the Narrative Shocks Missed

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Coibion updates the series, and the recent recession raises a hard question (Coibion, 2012):

## **An Omitted Motive Looks Like a Shock**

Large negative shocks mean cuts beyond what the forecasts justified. The Fed may have feared a financial crisis the regression omits.

Large stimulus before a slow recovery can then look ineffective.

# Which Timing Restriction Would You Defend?

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Every ordering so far rests on a claim about a single period.

## **Question**

Of Kilian's three timing restrictions, which would you defend? Which would you drop?

Take answers from the room.

## SECTION 4

# Long-Run Restrictions

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1. The Identification Problem
2. Recursive Identification
3. Monetary Policy Shocks
4. Long-Run Restrictions

# When Timing Restrictions Are Guesswork

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Recursive identification needs confident claims about one period. Often nobody has them:

- **Sometimes Defensible:** Oil output is physically slow; some data arrive with a lag.
- **Often Not:** Financial prices are set continuously, inside any period you pick.

## Theory Predicts the Long Run, Not the Impact

Theory predicts that a demand shock leaves long-run output unchanged. Theory rarely predicts impact effects.

# Restricting the Long Run Instead

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Theory pins down where the economy ends up, not how it gets there:

- **A Positive Demand Shock:** Long-run output is unchanged, and the price level rises.
- **A Supply Shock:** A permanent productivity gain raises the long-run level of output.

## **A Long-Run Restriction Zeroes a Cumulative Effect**

A long-run restriction sets one shock's total effect on one variable to zero. Impact effects are unrestricted.

# Long-Run Effects Are Summed Responses

A level ( $y_t$ ) changes by the running total of its growth rates ( $\Delta y_t$ ):

$$y_{t+h} - y_{t-1} = \sum_{j=0}^h \Delta y_{t+j} \quad (13)$$

## Summing Growth Responses Gives the Level Effect

A shock's responses are  $C$ , then  $BC$ ,  $B^2C$  and so on. Their running sum is its effect on the level.

# The Geometric Sum in Matrix Form

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Summing every response is a geometric sum, and it has a closed form:

$$D = (I + B + B^2 + \dots)C = (I - B)^{-1}C \quad (14)$$

where:

■  $D$ : long-run response matrix

■  $I$ : identity matrix

## Each Entry Is a Cumulative Effect

$d_{ij}$  is shock  $j$ 's cumulative effect on variable  $i$ . The sum converges when every eigenvalue of  $B$  lies inside the unit circle.

# The Blanchard–Quah Set-Up in Matrices

The long-run matrix is unknown, but  $DD'$  needs only least squares output:

$$DD' = (I - B)^{-1} \Sigma [(I - B)^{-1}]' \quad (15)$$

## Only the Product Is Estimated

Estimates fix  $DD'$ , as they fixed  $\Sigma$ . How  $DD'$  splits into  $D$  and its transpose is still open.

## RESIDUAL COVARIANCE MATRIX

## The Blanchard–Quah Long-Run Restriction

Two variables need one restriction, so assume  $D$  is lower triangular:

$$D = \begin{pmatrix} d_{11} & 0 \\ d_{21} & d_{22} \end{pmatrix} \quad (16)$$

- **The Zero:** The second shock has no long-run effect on the first variable.
- **What Stays Free:** The second shock may change the first variable for years.

### Lower Triangular Again, in a Different Place

A recursive scheme makes  $A_0$  lower triangular. A long-run scheme makes  $D$  lower triangular.

## Uniqueness Delivers the Impact Matrix

A lower-triangular  $D$  is the unique Cholesky factor of  $DD'$ , and  $C$  follows:

$$D = \text{chol}\left((I - B)^{-1}\Sigma[(I - B)^{-1}]'\right), \quad C = (I - B)D \quad (17)$$

### The Long Run Pins Down the Impact Effects

Restricting cumulative effects delivers  $C$ , so every impulse response follows. No timing assumption was needed.

## Supply and Demand Shocks, Identified

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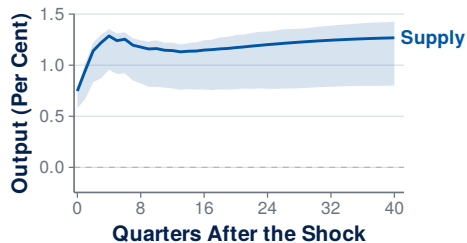
Blanchard and Quah applied the method to output growth and unemployment (O. J. Blanchard & Quah, 1989):

- **The Variables:** The log-difference of GDP, and the unemployment rate in levels.
- **The Labels:** The shock with a permanent output effect is supply, the other demand.
- **Their Finding:** Demand shocks account for most short-run output fluctuation.

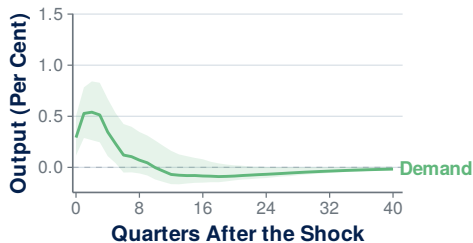
### The Labels Are Assumed, Not Discovered

Nothing in the data makes the permanent shock a supply shock. The restriction assigns the name.

# Supply and Demand Shocks on 1948–2019 Data



**Figure 5:** Supply shock: cumulative output response, 1948–2019.



**Figure 6:** Demand shock: cumulative output response, 1948–2019.

## **Demand Carries the Short Run, Supply the Level**

The demand shock's long-run output effect is zero by construction. The supply shock's settles near 1.3 per cent.

## Galí's Technology and Hours VAR

Galí orders productivity growth first, so only technology changes long-run productivity (Galí, 1999):

$$Z_t = (\Delta z_t, \Delta n_t)', \quad D = \begin{pmatrix} d_{11} & 0 \\ d_{21} & d_{22} \end{pmatrix} \quad (18)$$

where:

■  $\Delta z_t$ : growth of output per hour

■  $\Delta n_t$ : growth of hours worked

### A Technology Shock Changes What Labour Produces

Only a technology shock permanently changes output per hour. Both shocks' long-run effects on hours are free.

# Why Galí's VAR Tests the RBC Model

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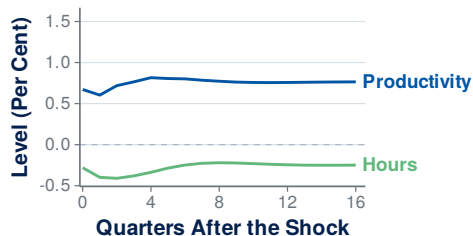
Real business cycle models make technology shocks the source of the cycle:

## **The RBC Model Predicts Hours Rise with Technology**

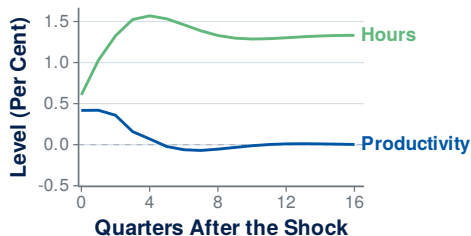
Working when you are productive beats working when you are not. A positive technology shock raises hours and output.

An identified VAR delivers the sign of the hours response directly.

# Responses to Technology and Non-Technology Shocks



**Figure 7:** Technology shock: productivity and hours, 1948–2019.



**Figure 8:** Non-technology shock: productivity and hours, 1948–2019.

## Hours Fall After a Positive Technology Shock

Productivity rises permanently, and hours are still lower four years on. The RBC model predicts hours rise.

## Reading Galí's Two Impulse Responses

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Neither shock produces what a technology-driven cycle predicts (Galí, 1999):

### **Demand-Determined Output Explains the Falling Hours**

More efficiency means demanded output needs less labour. Short-run output looks demand-driven.

Non-technology shocks raise output and productivity together in the short run.

# What Galí's Results Cost the RBC Model

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Galí's own interpretation runs against the real business cycle account (Galí, 1999):

- **Labour Adjustment Costs:** In a boom, work existing staff harder rather than hire.
- **In a Recession:** Employed labour is under-utilised, so measured productivity falls.

## The Hours Finding Is Contested

Later work specifies hours differently and gets different answers. The question is not settled.

# What Every Identification Scheme Shares

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Orderings, outside elasticities, narrative records and long-run restrictions all do one job:

- **The Common Job:** Each supplies from outside the sample what the residuals cannot.
- **The Common Cost:** Each restriction is an assumption the sample cannot test.

## Report the Scheme, Not Only the Responses

An impulse response without its identifying assumption is not a finding. The assumption is the claim.

## Before Lecture 1.4

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### 1 **Play:**

Re-identify last week's VAR under two orderings and compare the responses.

### 2 **Apply:**

Specify and identify one VAR, then save it for later weeks.

### 3 **Read:**

Whelan on latent variables, then Kilian's oil paper in full (Kilian, 2009).

Fix the VAR's series, sample, lag length, ordering and file, and keep all five.

## Next Lecture

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Lecture 1.4 turns to variables no dataset contains, and to the Kalman filter:

### 1 Unobserved Components.

Writing a model in state-space form.

### 2 The Kalman Filter.

Extracting a state you cannot see.

### 3 Estimation and Smoothing.

Estimating the variances, and revising the past.

### 4 The Natural Rate of Interest.

What the filter is used for.

# Thank you

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BACKUP

# Appendix

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# Notation

| Symbol          | What it is                       | First met                               |
|-----------------|----------------------------------|-----------------------------------------|
| $e_{it}$        | residual                         | Lecture 1.1                             |
| $A_0$           | within-period effects            | Lecture 1.2                             |
| $Z_t$           | vector of the $n$ variables      | Two Ways to Write the Same System       |
| $A_i$           | coefficients on lag $i$          | Two Ways to Write the Same System       |
| $p$             | number of lags                   | Two Ways to Write the Same System       |
| $n$             | number of variables              | Lecture 1.2                             |
| $\varepsilon_t$ | structural shock                 | Lecture 1.2                             |
| $C$             | impact matrix                    | Lecture 1.2                             |
| $B$             | reduced-form lag matrix          | One Lag Keeps the Algebra Short         |
| $\Sigma$        | residual covariance              | Lecture 1.2                             |
| $P$             | lower-triangular Cholesky factor | Cholesky Delivers the Triangular Matrix |
| $z_t$           | Kilian's three variables         | Kilian's Three-Variable Monthly VAR     |

# Notation

| Symbol                 | What it is                 | First met                             |
|------------------------|----------------------------|---------------------------------------|
| $\Delta \text{prod}_t$ | growth of world oil output | Kilian's Three-Variable Monthly VAR   |
| $\text{rea}_t$         | global real activity index | Kilian's Three-Variable Monthly VAR   |
| $\text{rpo}_t$         | real price of oil          | Kilian's Three-Variable Monthly VAR   |
| $\pi_t$                | inflation                  | Stock and Watson's Ordering           |
| $u_t$                  | unemployment               | Stock and Watson's Ordering           |
| $i_t$                  | funds rate                 | Stock and Watson's Ordering           |
| $y_t$                  | level                      | Long-Run Effects Are Summed Responses |
| $\Delta y_t$           | growth rates               | Long-Run Effects Are Summed Responses |
| $D$                    | long-run response matrix   | The Geometric Sum in Matrix Form      |
| $I$                    | identity matrix            | The Geometric Sum in Matrix Form      |
| $\Delta z_t$           | growth of output per hour  | Galí's Technology and Hours VAR       |
| $\Delta n_t$           | growth of hours worked     | Galí's Technology and Hours VAR       |

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